

## Average life of radioactive nuclei and Numericals

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### Average Life period of nuclei ( $\tau$ )

The statistical average of the lives of all atoms present at any time is called the average life.

Units : time

Equation  $\tau = \frac{1}{\lambda}$  OR  $\tau = 1.44 \times t_{1/2}$

Numerical Problems

**1) Half life period of a radioactive element is 10 years. Calculate its disintegration constant & average life?**

**Solution**

**Data given**

$$t_{1/2} = 10 \text{ years}$$

$$\lambda = ?$$

$$\tau = ?$$

$$\lambda = 0.693 / t_{1/2}$$

$$= 0.693 / 10$$

$$\lambda = 0.0693 \text{ years}^{-1}$$

$$\tau = 1.44 \times t_{1/2}$$

$$= 1.44 \times 10$$

$$\tau = 14.4 \text{ years}$$

2) Half life of  ${}_{83}\text{I}^{125}$  is 60 days. How much of its radioactivity remains after 180 days ?

**Solution**

**Data given**

$$t_{1/2} = 60 \text{ days ,}$$

$$t = 180 \text{ days}$$

$$N_0 = 1 \text{ g}$$

$$N_t = ?$$

$$\lambda = \frac{0.693}{t_{1/2}}$$

$$= 0.693/60$$

$$\lambda = 0.01155 \text{ days}^{-1}$$

$$\lambda = \frac{2.303}{t} \log \frac{N_0}{N_t}$$

$$0.01155 = \frac{2.303}{180} \log \frac{1}{N_t}$$

$$\log \frac{1}{N_t} = 0.9027$$

$$\frac{1}{N_t} = 7.993$$

$$N_t = 0.125 \text{ g}$$

3) Half life period of a radioactive element is 35 Hours. Calculate its disintegration constant & the time required to reduce by 63% of its initial activity?

**Solution**

**Data given**

$$t_{1/2} = 35 \text{ Hours}$$

$$N_0 = 100 \%$$

$$N_t = 100 - 63 = 37 \%$$

$$\lambda = ?$$

$$t = ?$$

$$\lambda = 0.693 / t_{1/2}$$

$$= 0.693 / 35$$

$$\lambda = 0.0198 \text{ Hours}^{-1}$$

$$\lambda = \frac{2.303}{t} \log \frac{N_0}{N_t}$$

$$0.0198 = \frac{2.303}{t} \log \frac{100}{37}$$

$$t = \frac{2.303}{0.0198} \log 2.703$$

$$t = 116.31 \times 0.4318$$

$$t = 50.22 \text{ Hours}$$