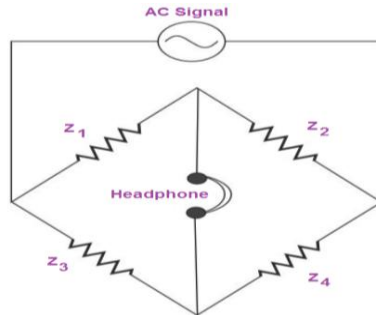


## AC Bridges

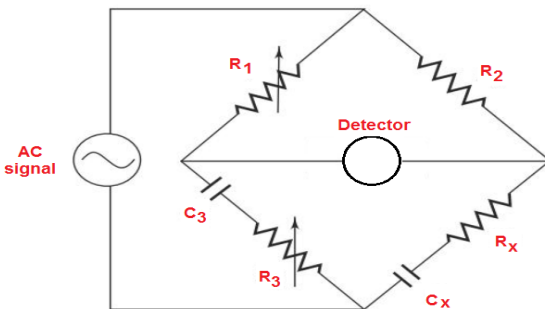
- Bridge circuit is operated (excited) with only AC voltage signal.
- AC bridges are used to measure the value of unknown inductance, capacitance and frequency.
- AC bridge has **four arms** and each arm consists of some impedance. Each arm will be having either single or combination of passive elements such as resistor, inductor and capacitor.



$$\frac{Z_1}{Z_2} = \frac{Z_3}{Z_4}$$

Necessary to adjust both the magnitude and phase angles of the impedance arms to achieve balance, i.e. the bridge must be balanced for both the reactance and the resistive component.

### CAPACITANCE COMPARISON BRIDGE



The equation for balanced condition is

$$Z_1 Z_x = Z_2 Z_3$$

The capacitive balance gives

$$C_x = \frac{C_3 R_1}{R_2}$$

The resistive balance gives

$$R_x = \frac{R_2 R_3}{R_1}$$

The ratio arms  $R_1$ ,  $R_2$  are resistive. The known standard capacitor  $C_3$  is in series with  $R_3$ .  $R_3$  may also include an added variable resistance needed to balance the bridge.  $C_x$  is the unknown capacitor and  $R_x$  is the small leakage resistance of the capacitor. In this case an unknown capacitor is compared with a standard capacitor and the value of the former, along with its leakage resistance. A fixed resistance ratio and variable standards are used. Balance is obtained by alternately varying  $C_3$  and  $R_3$

$$Z_1 = R_1$$

$$Z_2 = R_2$$

$$Z_3 = R_3 - \frac{j}{\omega C_3}$$

$$Z_x = R_x - \frac{j}{\omega C_x}$$

The condition for balance of the bridge is

$$Z_1 Z_x = Z_2 Z_3$$

$$R_1 \left( R_x - \frac{j}{\omega C_x} \right) = R_2 \left( R_3 - \frac{j}{\omega C_3} \right) \quad (1)$$

$$R_1 R_x - \frac{R_1 j}{\omega C_x} = R_2 R_3 - \frac{R_2 j}{\omega C_3}$$

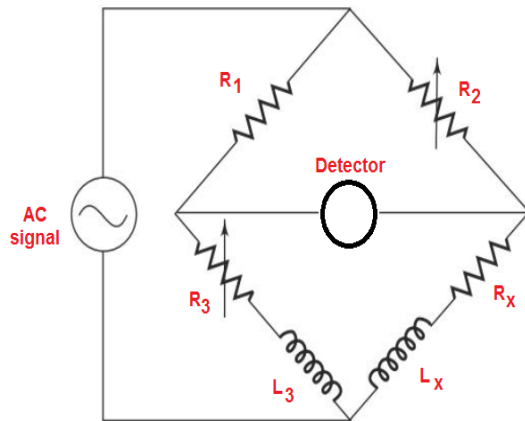
Two complex quantities are equal when both their real and their imaginary terms are equal.

$$R_1 R_x = R_2 R_3 \quad \text{and} \quad \frac{R_2}{\omega C_3} = \frac{R_1}{\omega C_x} \quad (2)$$

$$C_x = \frac{C_3 R_1}{R_2}$$

$$R_x = \frac{R_2 R_3}{R_1}$$

## INDUCTANCE COMPARISON BRIDGE



The equation for balanced condition is

$$Z_1 Z_x = Z_2 Z_3$$

The inductive balance gives

$$L_x = \frac{L_3 R_2}{R_1}$$

The resistive balance gives

$$R_x = \frac{R_2 R_3}{R_1}$$

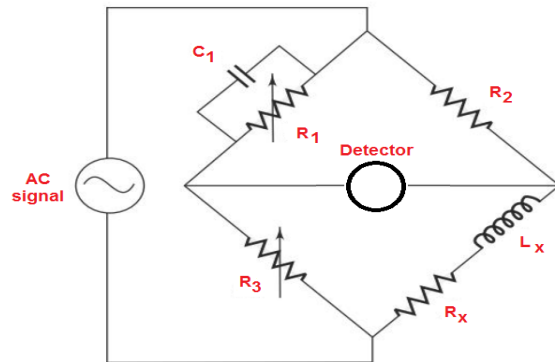
Value of the unknown inductance  $L_x$  and its internal resistance  $R_x$  are obtained by comparison with the standard inductor and resistance, i.e.  $L_3$  and  $R_3$ .

$R_2$  is chosen as the inductive balance control and  $R_3$  as the resistance balance control.

Balance is obtained by alternately varying  $L_3$  or  $R_3$ .

If the  $Q$  of the unknown reactance is greater than the standard  $Q$ , it is necessary to place a variable resistance in series with the unknown reactance to obtain balance.

## MAXWELL BRIDGE



$$R_x = \frac{R_2 R_3}{R_1}$$

$$L_x = C_1 R_2 R_3$$

$$Q = \omega C_1 R_1$$

Maxwell's bridge measures an unknown inductance in terms of a known capacitor. One arm has a resistance  $R_1$  in parallel with  $C_1$  and hence it is easier to write the balance equation using the admittance of arm 1 instead of the impedance.

- Used for inductance measurements of low Q.
- Best suited since comparison with a capacitor is more ideal than with an inductor
- Measure from 1  $\mu\text{H}$  to 1000 H with an accuracy of  $\pm 2\%$  ( $Q < 10$ )

The condition for balance of the bridge is

$$Z_1 Z_x = Z_2 Z_3$$

$$Z_x = \frac{Z_2 Z_3}{Z_1} = Z_2 Z_3 Y_1 \quad (1)$$

$$Z_1 = \frac{1}{R_1} + j\omega C_1 \quad (R_1 \text{ in parallel with } C_1)$$

$$Z_2 = R_2$$

$$Z_3 = R_3$$

$$Z_x = R_x + j\omega L_x$$

From eq.1 we have

$$(R_x + j\omega L_x) = R_2 R_3 \left( \frac{1}{R_1} + j\omega C_1 \right) \quad (2)$$

$$R_x + j\omega L_x = \frac{R_2 R_3}{R_1} + j\omega C_1 R_2 R_3$$

Equating real and imaginary terms we have

$$R_x = \frac{R_2 R_3}{R_1} \quad \text{and} \quad L_x = C_1 R_2 R_3 \quad (3)$$

$$Q = \frac{\omega L_x}{R_x} = \frac{\omega C_1 R_2 R_3 R_1}{R_2 R_3} = \omega C_1 R_1 \quad (4)$$