

Quadrant II – Transcript and Related Materials

Programme: Bachelor of Science (Second Year)

Subject: Physics

Paper Code: PYS101

Paper Title: Network Analysis

Unit: 3 Transient Response of RL and RC circuits and RLC circuit to DC and AC signals

Module Name: Sinusoidal response of RLC circuit.

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Transcript

Welcome students. The program is Bachelor of Science, second year

Subject Physics Semester three.

Paper code PYS 101

Paper title Network analysis

Unit Three Response of RL, RC and RLC Circuit to DC and AC

Module name. Sinusoidal response of RLC circuit.

Module number 18

I'm Efrem D'Sa from Camel College of Art, Science and Commerce for women.

The outline is AC analysis of RLC circuit.

Voltage equations for RLC circuit,

Solution for RLC circuit and its interpretation.

Learning outcomes

Apply Kirchoff's Voltage law to series RLC circuit.

Determine impedance phase relationship between voltage and current in a series RLC circuit.

Understand the variation in impedance, phase angle with frequency.

First The sinusoidal response of RLC circuit.

If the voltage $V(t)$ and current $I(t)$ be the instantaneous values of voltage and current. And writing Kirchoff's voltage law for the close circuit,

we have $V(t)$ is equal to the current into the resistance plus the voltage across inductance plus the voltage across capacitance.

As V_L , the voltage across inductance is equal to $L \frac{dI}{dt}$.

And the voltage across the capacitance is equal to $\frac{1}{C} \int I(t) dt$.

We, if it take the current AC current $I(t)$ to be $I_m \sin \omega t$

Then the voltage as a function of time is given by substituting the current $I(t)$ in this expression, which gives us on differentiating and integrating gives us $R I_m \sin \omega t + \omega L I_m \cos \omega t - I_m \text{ divided by } \omega C \cos \omega t$.

Now this is a trigonometric method of the solution, now this method becomes complex and tedious. So we use other simpler methods.

Like Phasor method, j operator method and complex method.

Using j operator method, that is complex number method.

Here we define j operator which operates on a vector to effectively rotate it by 90 degrees and minus j operator by minus 90 degrees without any change in magnitude to the vector. So if you consider the current $i(t)$ to be a complex corresponding to a complex voltage $V(t)$

Since the voltage across inductor leads the current by 90 degrees,

and j that will be multiplied by j to indicate this 90 degrees

and the voltage across the capacitor lags current by minus 90 degrees.

so multiplied by minus j OK to represent the lag of current.

So using the j operator method. we simply write the voltage at anytime t is equal to the current $I(t)$ into the resistance plus j times

ωL into the current minus j times the current divided by ωC

Here we can easily write voltage as a function of time is equal to the

current as a function in bracket $R + j \omega L - j \text{ into one by } \omega C$

where if I right for the Z vector impedance, Z is equal to $V(t)/I(t)$, then the

impedance vector is given by $R + j \text{ in bracket } \omega L - \text{ one by } \omega C$.

The magnitude of Z is the square root of the vector impedance

square root of $R^2 + \omega L^2 - \frac{1}{\omega C^2}$ the whole square.

The magnitude of circuit current I_t is given by the voltage divided by the magnitude of the vector impedance α the phase angle by which the

applied voltage leads or lags the current or the phase difference between the applied voltage and current is given by the relation.

α is $\tan^{-1} \left(\frac{\omega L - \frac{1}{\omega C}}{R} \right)$ the whole divided by R .

The magnitude of Z , phase angle α and the magnitude of current I_t vary with frequency of applied voltage.

We can consider 3 cases.

One is when ωL minus $1/\omega C$ is greater than 0.

When ωL minus $1/\omega C$ is less than zero and

3rd when ωL minus $1/\omega C$ is equal to 0.

The case one ωL minus $1/\omega C$ is greater than zero.

The net reactance is positive that is inductive, α is positive and the applied voltage v_t leads the circuit current I_t by a phase angle α .

That is voltage lags the current by a phase angle α is equal to

$\tan^{-1} \frac{1}{\omega C R}$.

So I have again the case one here

The net reactance is positive that is inductive α is positive applied voltage v_t leads the circuit current I_t by a phase angle α . The impedance Z here is greater than equal to R .

In case of ωL being greater very much greater than $1/\omega C$ that is at high frequency.

The RLC circuit acts like an RL circuit with Z is equal to ωL and α is 90 degrees.

Case 2 ωL less than $1/\omega C$,

the net reactance is capacitive, α is negative, applied voltage V_t lags the circuit current I_t by a phase angle α .

The impedance here Z is again greater than R .

If ωL is very much smaller compared to $1/\omega C$ that is for very low frequencies.

The RLC circuit acts like an RC circuit and that is equal to $1/\omega C$ and α is minus 90 degrees.

Case 3. ωL minus $1/\omega C$ is equal to 0.

That is, ωL is equal to $1/\omega C$, here the net reactance is 0, α is zero, applied voltage that is in phase with the circuit current I_t with α equal to 0.

The impedance is purely resistive Z minimum is equal to R .

The maximum current flows through the circuit, phase difference 0, ωL is equal to $1/\omega C$ indicates a series resonant

with resonance frequency ω_0 square equal to $1/LC$
or frequency f_0 is equal to $1/2\pi \sqrt{LC}$

The notations used as shown in the slide.
References as shown in this slide.

Thank you.